

Practice Exercises N 1+ correction

Exercise 1: Convert the following numbers:

$$(32)_8 = (?)_2 = (?)_{16}$$

$$(18)_{10} = (?)_8 = (?)_{16}$$

$$(A01)_{16} = (?)_2 = (?)_8$$

$$(101101,01)_2 = (?)_8 = (?)_{10} = (?)_{16}$$

Exercise 2

1. The number (10101010) is represented in 2's complement. What is its decimal value?
2. Calculate in binary (2's complement on 8 bits) : 30-12.

Exercise 3

1. Convert π to binary (base 2) (with the approximation $\pi = 3.125$)
2. Code $\pi = 3.125$ according to IEEE 754 standard (single precision) and give the result in Hexadecimal form.
3. Deduce $-\pi$.

Exercise 4

The number $X = (C0\ D4\ 00\ 00)_{16}$ is coded according to IEEE 754 Standard - single precision

What is the decimal value of X ?

Correction

Exercise 1 :

$$(32)_8 = (011010)_2 = (1A)_{16}$$

$$(18)_{10} = (22)_8 = (12)_{16}$$

$$(A01)_{16} = (1010\ 0000\ 0001)_2 = (5001)_8$$

$$(101101,01)_2 = (55,2)_8 = (45,25)_{10} = (2D,4)_{16}$$

Exercise 2 :

1. The number (10101010) is represented in C à 2

To find its value in decimal, simply transform it into decimal but multiply the most significant bit by -1 (the most significant bit (in red) = 1 means that the number is negative.

$$\begin{aligned} \underline{1}0101010 &= 2^0*0 + 2^1*1 + 2^2*0 + 2^3*1 + 2^4*0 + 2^5*1 + 2^6*0 + 2^7*(-1) \\ &= 2 + 8 + 32 - 128 \\ &= (-86)_{10} \end{aligned}$$

2. Let's calculate 30-12 in binary in C to 2 on 8 bits:

$$30-12 = 30 + (-12)$$

Alors :

$$30 = (00011110)_2$$

Now let's represent (-12) in binary (using the C to 2) $12 = (00001100)_2$

$$\text{So } (-12) = (11110100)_2$$

Therefore :

$$30-12 = 00011110 + 11110100 = (00010010)_2$$

Exercise 3

1. $\pi = (3.125) = (11.001)_2$
2. Coding of π according to IEEE 754 standard

$$11.001 = 1.1001 * 2^1 \square \text{d\u00e9calage} = 1$$

$$E = 127 + 1 = (128)_{10} = (10000000)_2$$

$$S = 0$$

$$E = 10000000$$

M = 1001 . We add zeros to represent M sur 23 bit

$$(3.125)_{10} = (01000000100100000000000000000000)_2$$

$$= (40480000)_{16}$$

4. Deduce $-\pi$ (just change the sign bit S)

$$\Pi = 01000000100100000000000000000000_2$$

$$-\Pi = (11000000100100000000000000000000)_2$$

$$= (C0480000)_{16}$$

Exercice 4 :

Simply decode the number into binary to extract the components: S, E, M

$$X = (C0 D4 00 00)_{16}$$

$$= (1100 0000 1101 0100 0000000000000000)_2$$

S = 1 so x is negative

$$E = (10000001)_2 = 129 \text{ dec} = 2$$

$$X = -1.10101 * 2^2 = (110.101)_2$$

$$X = (-6.625)_{10}$$