

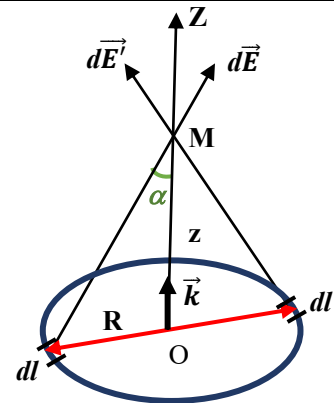
**SERIES 2 (Part 2)**

***(Continuous Distribution of Charges, Gauss's Theorem, Conductors)***

**Exercise 1 :**

Consider a circular wire of radius  $R$ , uniformly charged with a charge density  $\lambda > 0$ .

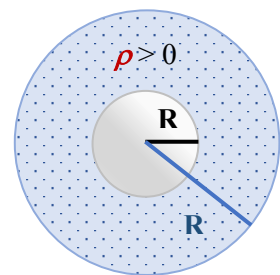
1. Determine the electric field  $\vec{E}(M)$  created at a point  $M$  on its axis, located at a distance  $z$  from center  $O$ .
2. Give the expression of the electric potential  $V(M)$ .
3. Deduce  $\vec{E}(M)$ .



**Exercise 2 :**

Let two concentric spheres with center  $O$  of radii  $R_1$  and  $R_2$  respectively such that  $R_1 < R_2$ .

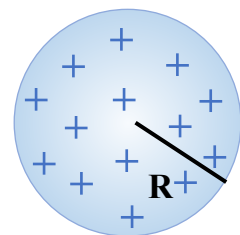
1. Using Gauss's theorem, calculate the electrostatic field at any point in space for a volume charge distribution ( $\rho > 0$ ) uniformly distributed between these two spheres.
2. Deduce the electric potential at any point in space.



**Exercise 3 :**

A conducting sphere of radius  $R$  carries a charge  $Q > 0$ . Calculate:

1. Its potential  $V$ .
2. Its capacitance  $C$ .
3. Its surface density  $\sigma$ .



**Exercise 4 :**

Two conducting spheres, of radii  $R_1$  and  $R_2$  carrying charges  $Q_1$  and  $Q_2$  respectively, are placed at a very large distance compared to the radii.

1. Calculate the potentials  $V_1$  and  $V_2$  of the two spheres.
2. Connecting the two spheres with a conductive wire of negligible resistance, calculate the charges  $Q_1'$  and  $Q_2'$  as well as the potentials  $V_1'$  and  $V_2'$ .
3. Calculate the capacitance of the single conductor formed.