

Exercice Series N° 1

Exercise 1: Euclidean Distance

In pattern recognition, the Euclidean distance is calculated between two vectors  $X = x_i$  and  $Y = y_i$  with  $i = 1, \dots, N$  as follows

$$d(x, y) = \sqrt{(x_i - y_i)^2}$$

write a script in R for the Euclidean distance calculation of two vectors X and Y.

Exercise 2: Binary Similarity measures

Binary similarity measures are a set of similarity measures calculated between binary vectors. These similarities employ a 2\*2 contingency matrix with OTU (Operational Taxonomic Units). In a binary vector, 1 denotes the presence of the attribute and 0 denotes its absence. The OTU based matrix is calculated as follow for the Vectors  $X_i Y_j$

$j \setminus i$	1 (Presence)	0 (Absence)	Sum
1 (Presence)	$a = i \bullet j$	$b = \bar{i} \bullet j$	$a+b$
0 (Absence)	$c = i \bullet \bar{j}$	$d = \bar{i} \bullet \bar{j}$	$c+d$
Sum	$a+c$	$b+d$	$n=a+b+c+d$

Write a script in R to calculate the matrix and based on it the following two binary similarity measures

$$S_{JACCARD} = \frac{a}{a+b+c}$$

$$S_{ROGER\&TANIMOTO} = \frac{a+d}{a+2(b+c)+d}$$

Exercise 3: Cooccurrence matrix of a grey-level image

A grey-level image is an  $m \times n$  matrix of integer values within the range of  $[0, 255]$ . Cooccurrence matrix is a square matrix of  $256 \times 256$  used to calculate several image features such as texture statistical features.

Each element  $x_{ij}$  of the cooccurrence matrix present the apparition frequency of  $i^{th}$  grey level in adjacency with the  $j^{th}$  one for a certain direction  $\theta$ . The following example illustrates the calculation of matrix for a 4\*4 image with  $\theta = 0^\circ$ .

$$\begin{array}{cccc} 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 2 & 2 & 3 \\ 2 & 2 & 3 & 3 \end{array} \quad P_{0^\circ, 1} = \begin{bmatrix} 6 & 2 & 1 & 0 \\ 2 & 2 & 0 & 0 \\ 1 & 0 & 4 & 2 \\ 0 & 0 & 2 & 2 \end{bmatrix}$$

Write a script in R to calculate the cooccurrence matrix